

The saga of the Shastry- Sutherland compound $\text{SrCu}_2(\text{BO}_3)_2$

F. Mila

Ecole Polytechnique Fédérale de Lausanne
Switzerland

Collaborators

Theorists

S. Miyahara (Fukuoka), F. Becca (Trieste)
M. Moliner, (Lausanne), I. Rouschatzakis (Loughborough)
K. Schmidt and C. Boos (Erlangen), J. Dorier (Lausanne)
S. Manmana (Göttingen), A. Honecker (Cergy-Pontoise)
P. Corboz, S. Crone and I. Niesen (Amsterdam)
D. Badrtdinov and V. Mazurenko (Ekaterinburg)
B. Normand (PSI), S. Wessel (Aachen)

Experimentalists

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C. Berthier, M. Horvatic (Grenoble)
S. Haravifard (Duke)
H. Rønnow (Lausanne), C. Rüegg (PSI)

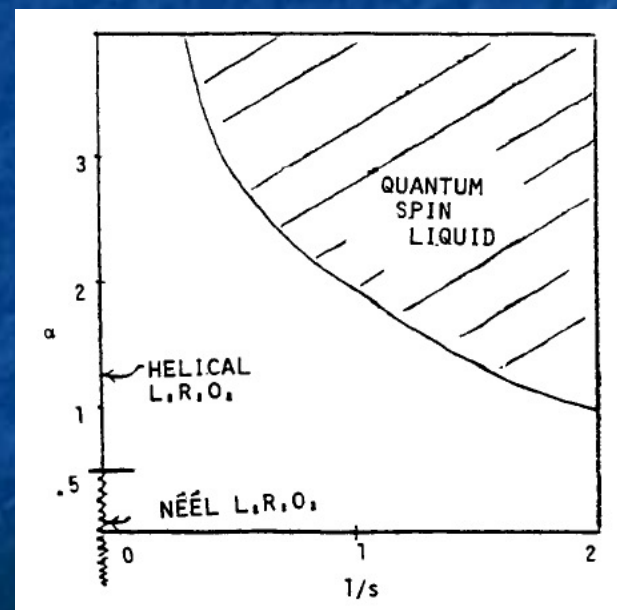
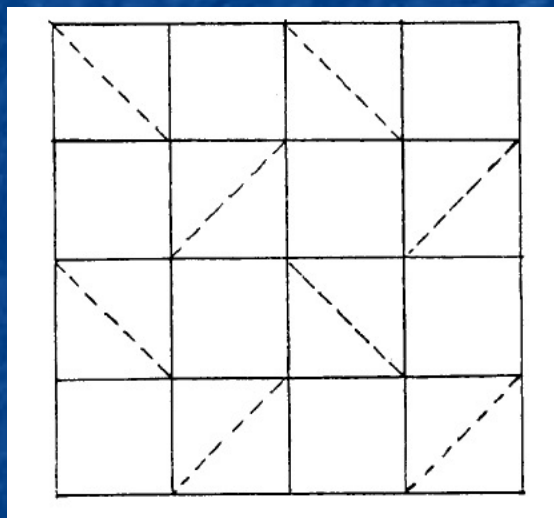
Scope

- The pioneers
Shastry-Sutherland 1981, Smith-Keszler 1991
- Magnetization plateaus of $\text{SrCu}_2(\text{BO}_3)_2$
Kageyama et al 1999, Kodama et al 2002, ...
- Intermediate phase of $\text{SrCu}_2(\text{BO}_3)_2$ under pressure
Waki et al 2007, Radtke et al 2014, ...
- Topological magnons
Romhanyi et al 2015, McClarty et al 2017
- Plaquette-AF transition
Lee et al 2019, Guo et al 2020
- First-order transition and critical point
Larrea et al 2021
- Bound states, impurities, combining magnetic field with pressure, spin supersolid, spin nematic, ...

EXACT GROUND STATE OF A QUANTUM MECHANICAL ANTIFERROMAGNET

B. Sriram Shastry and Bill Sutherland

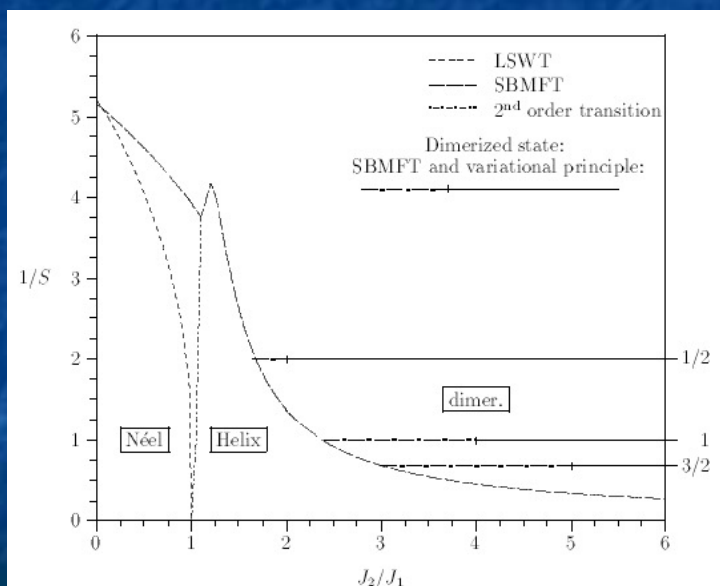
Department of Physics, University of Utah, Salt Lake City, UT 84112



First-order transition between magnetic order and valence bond order in a 2D frustrated Heisenberg model

M. ALBRECHT and F. MILA

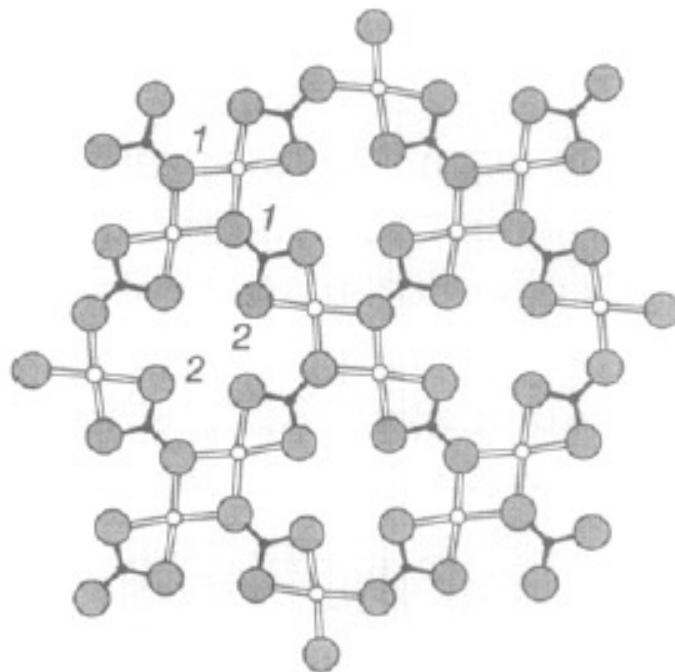
Laboratoire de Physique Quantique, Université Paul Sabatier - 31062 Toulouse, France



Synthesis, Structure, and Properties of the Orthoborate $\text{SrCu}_2(\text{BO}_3)_2$

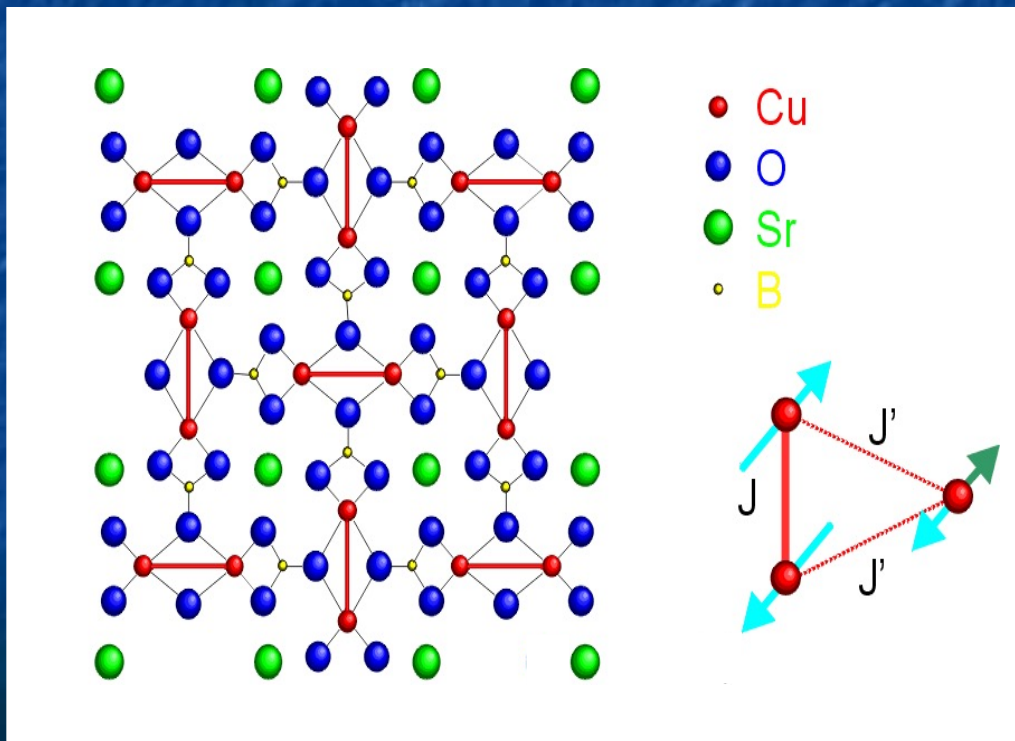
ROBERT W. SMITH AND DOUGLAS A. KESZLER*

*Department of Chemistry and Center for Advanced Materials Research,
Oregon State University, Gilbert Hall 153, Corvallis, Oregon 97331-4003*



$\text{SrCu}_2(\text{BO}_3)_2$

Smith and Keszler, JSSC 1991

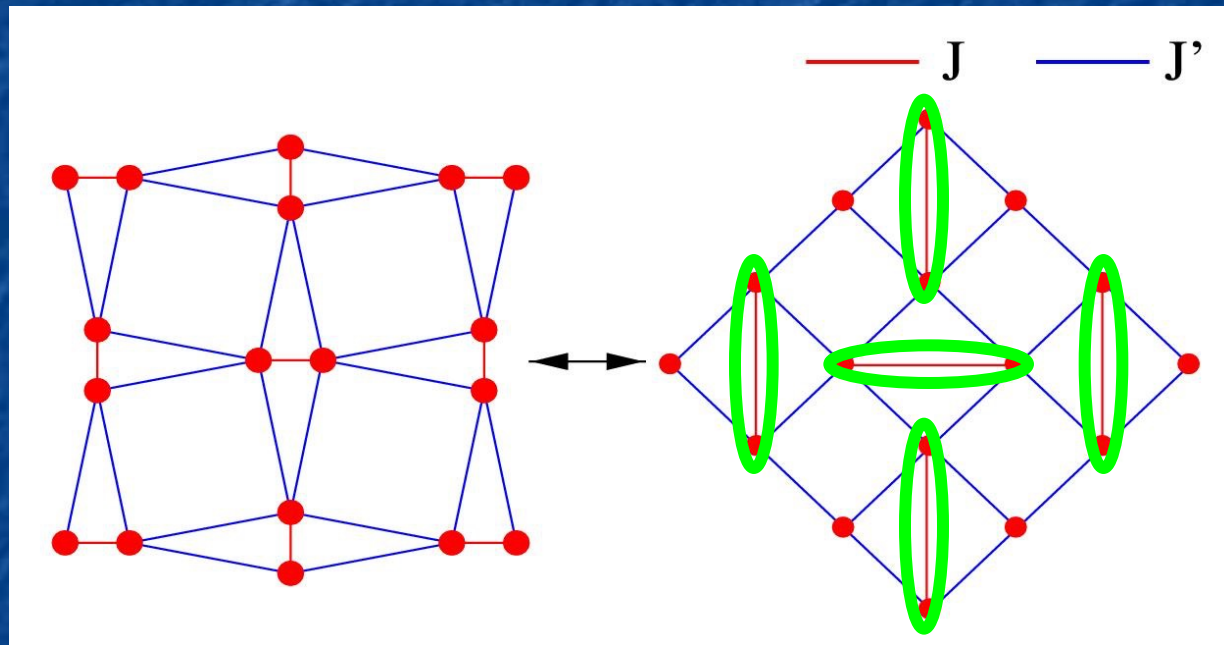


$\text{Cu}^{2+} \rightarrow \text{Spin } 1/2$

$J \approx 85 \text{ K}$

$J'/J \approx 0.63$

Shastry-Sutherland model



Ground-state = Product of singlets on J-bonds

Shastry and Sutherland, '81

→ Spin gap, and plateau at 0

Scope

- The pioneers

Shastry-Sutherland 1981, Smith-Keszler 1991

- **Magnetization plateaus of $\text{SrCu}_2(\text{BO}_3)_2$**

Kageyama et al 1999, Kodama et al 2002, ...

- Intermediate phase of $\text{SrCu}_2(\text{BO}_3)_2$ under pressure

Waki et al 2007, Radtke et al 2014, ...

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Lee et al 2019, Guo et al 2020

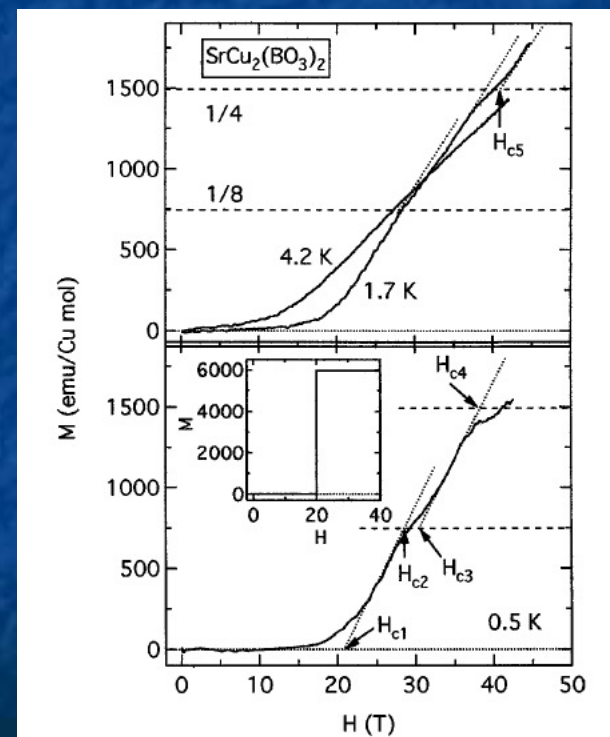
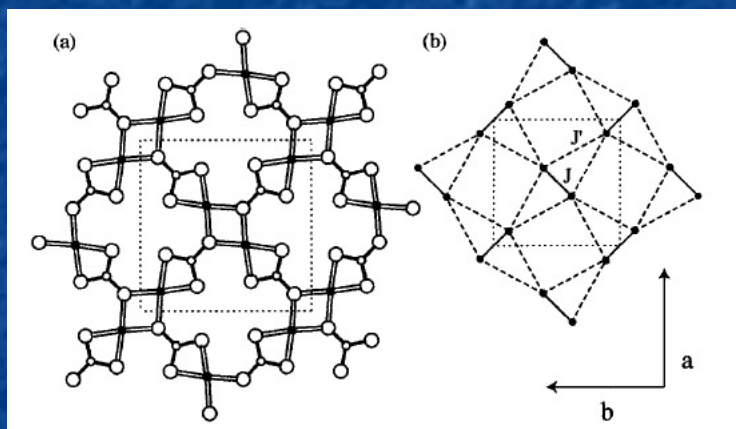
- First-order transition and critical point

Larrea et al 2021

- Bound states, impurities, combining magnetic field with pressure, spin supersolid, spin nematic, ...

Exact Dimer Ground State and Quantized Magnetization Plateaus in the Two-Dimensional Spin System $\text{SrCu}_2(\text{BO}_3)_2$

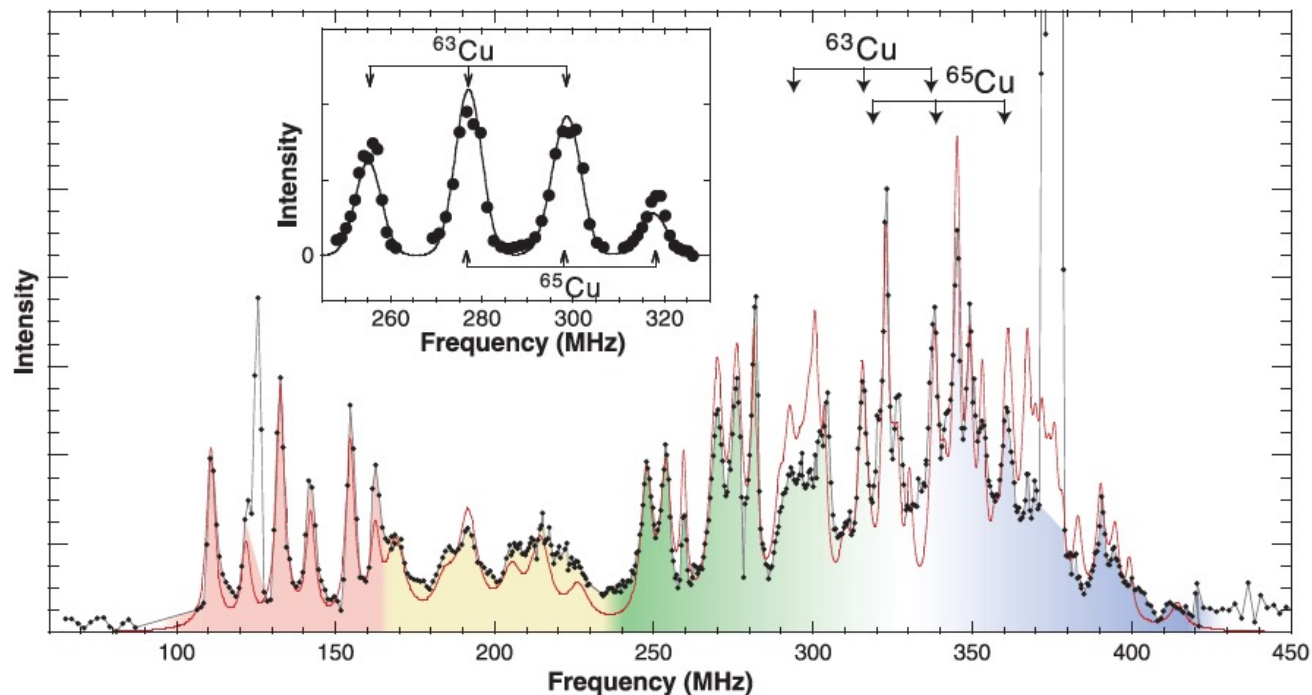
H. Kageyama,^{1,2,*} K. Yoshimura,^{1,3,†} R. Stern,³ N. V. Mushnikov,² K. Onizuka,² M. Kato,¹ K. Kosuge,¹
C. P. Slichter,³ T. Goto,² and Y. Ueda²



Magnetic Superstructure in the Two-Dimensional Quantum Antiferromagnet $\text{SrCu}_2(\text{BO}_3)_2$

K. Kodama,¹ M. Takigawa,^{1*} M. Horvatić,² C. Berthier,^{2,3}
H. Kageyama,¹ Y. Ueda,¹ S. Miyahara,^{1,4} F. Becca,⁴ F. Mila⁴

SCIENCE VOL 298 11 OCTOBER 2002

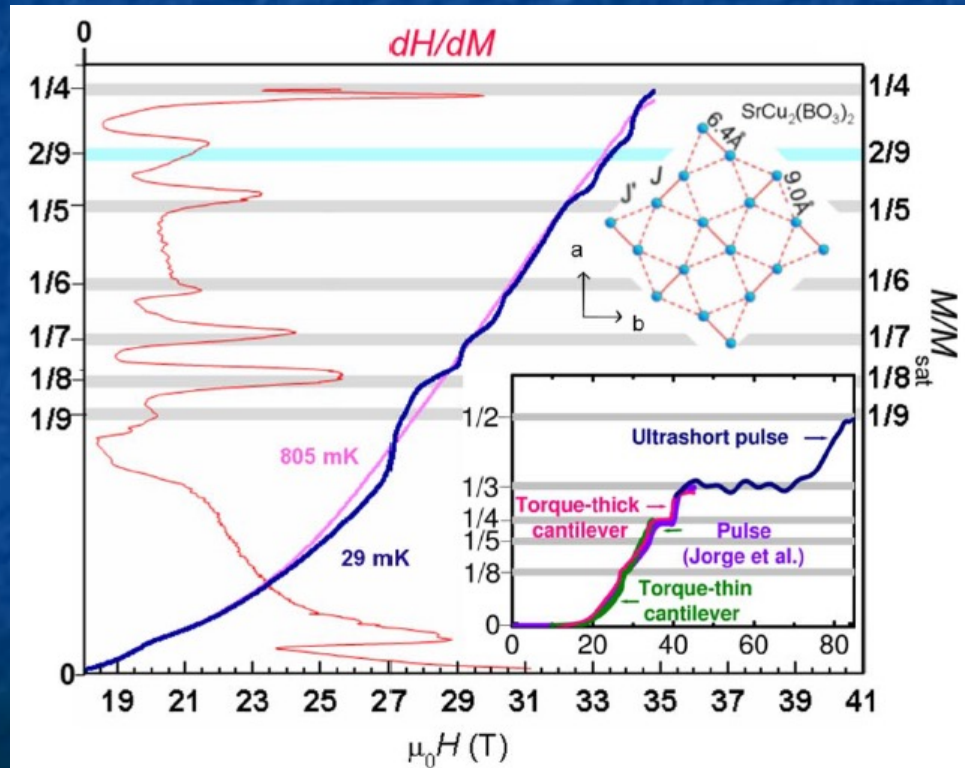


Fractalization drives crystalline states in a frustrated spin system

Suchitra E. Sebastian^{a,1}, N. Harrison^b, P. Sengupta^c, C. D. Batista^c, S. Francoual^b, E. Palm^d, T. Murphy^d, N. Marciano^a, H. A. Dabkowska^e, and B. D. Gaulin^e

www.pnas.org/cgi/doi/10.1073/pnas.0804320105

PNAS | December 23, 2008 | vol. 105 | no. 51 | 20157–20160

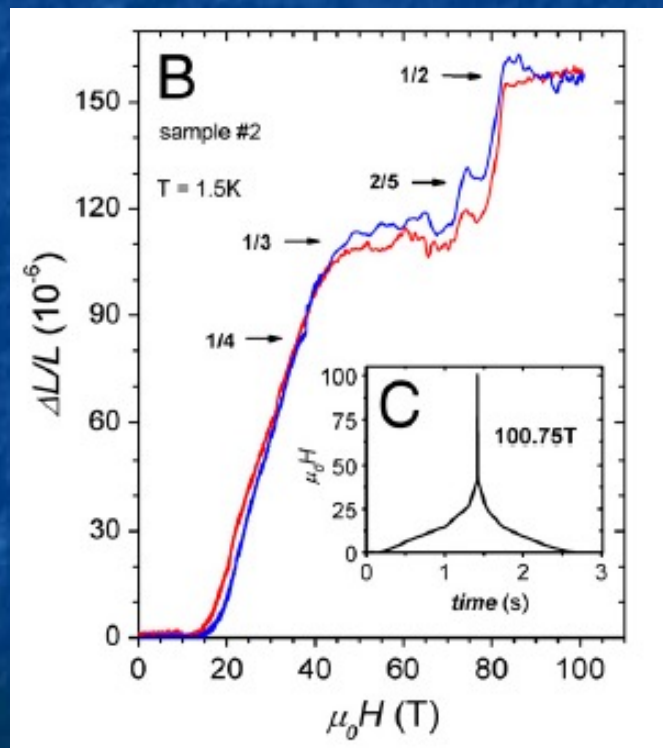


$1/9, 1/8, 1/7, 1/6,$
 $1/5, 2/9, 1/4$

Magnetostriction and magnetic texture to 100.75 Tesla in frustrated $\text{SrCu}_2(\text{BO}_3)_2$

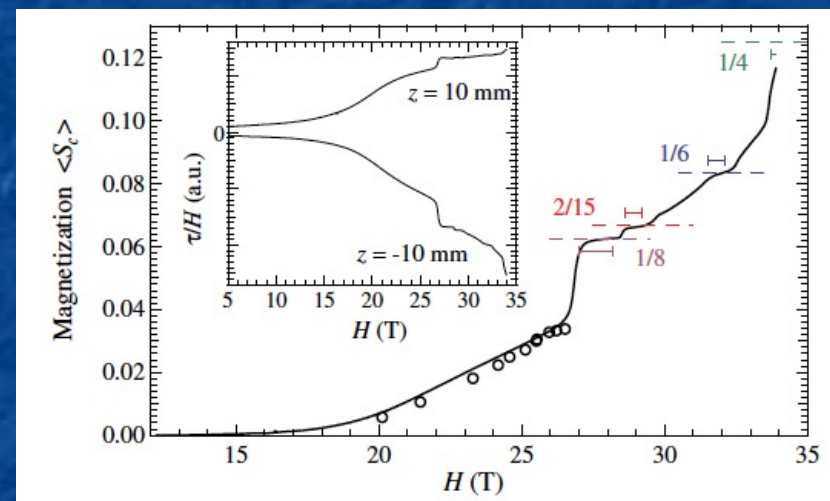
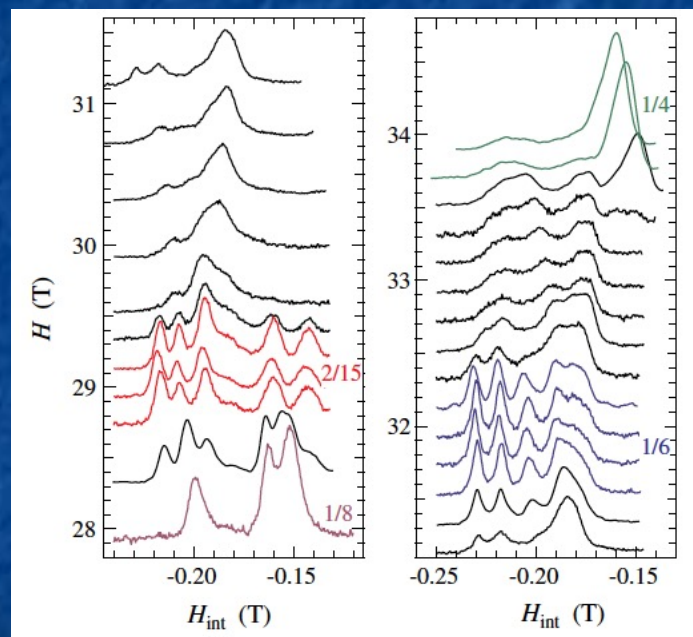
Marcelo Jaime^{a,b,1}, Ramzy Daou^{c,d}, Scott A. Crooker^{a,b}, Franziska Weickert^b, Atsuko Uchida^{a,b}, Adrian E. Feiguin^e, Cristian D. Batista^f, Hanna A. Dabkowska^g, and Bruce D. Gaulin^{g,h}

PNAS | July 31, 2012 | vol. 109 | no. 31



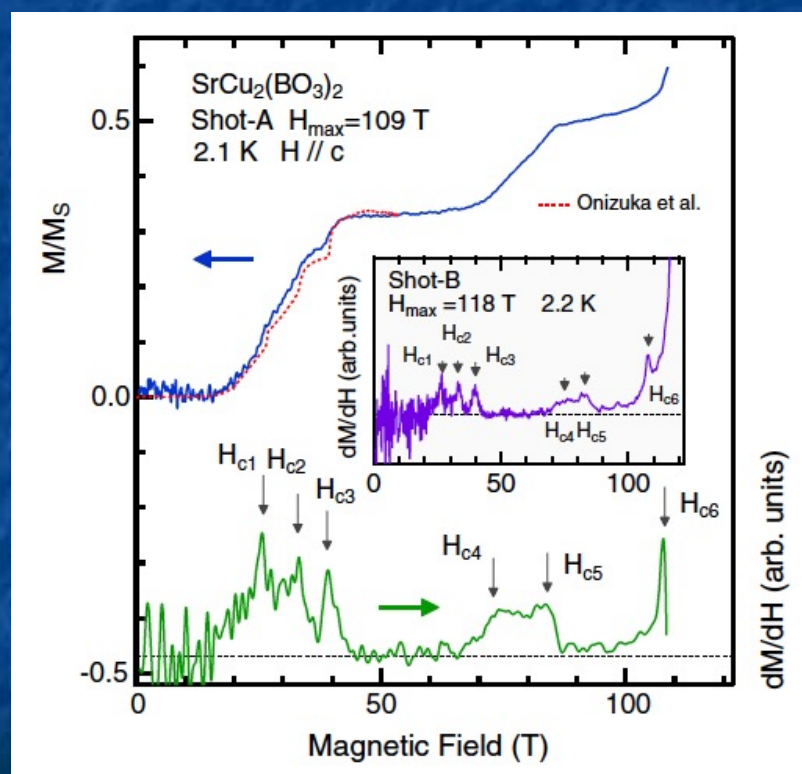
Incomplete Devil's Staircase in the Magnetization Curve of $\text{SrCu}_2(\text{BO}_3)_2$

M. Takigawa,^{1,*} M. Horvatić,² T. Waki,³ S. Krämer,² C. Berthier,² F. Lévy-Bertrand,^{2,†} I. Sheikin,² H. Kageyama,⁴
Y. Ueda,¹ and F. Mila⁵



Magnetization of $\text{SrCu}_2(\text{BO}_3)_2$ in Ultrahigh Magnetic Fields up to 118 T

Y.H. Matsuda,^{1,*} N. Abe,¹ S. Takeyama,¹ H. Kageyama,² P. Corboz,³ A. Honecker,^{4,5} S.R. Manmana,⁴
G.R. Foltin,⁶ K.P. Schmidt,⁶ and F. Mila⁷



Summary on plateaus

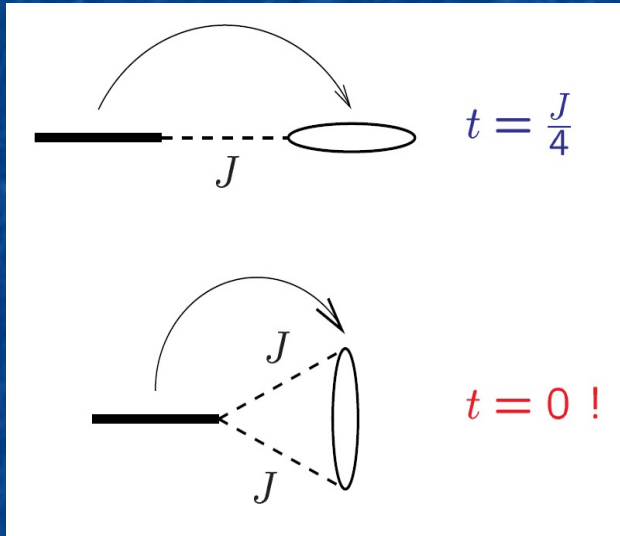
Improbable sequence of plateaus

$1/8$ $2/15$ $1/6$ $1/4$ $1/3$ $2/5$ $1/2$

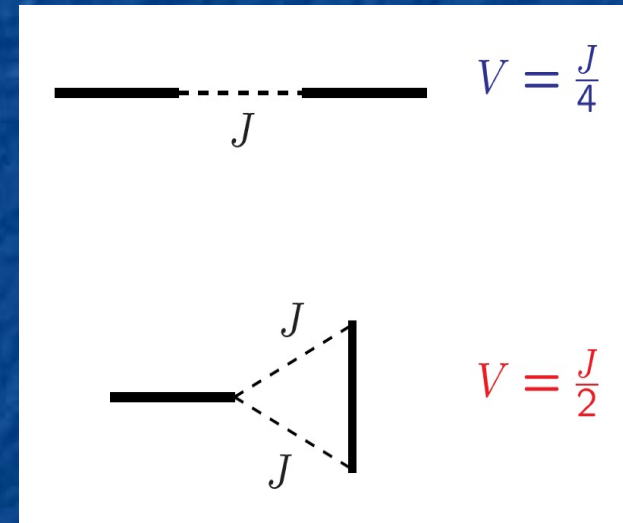
Theory?

Effect of frustration

Triplet Hopping



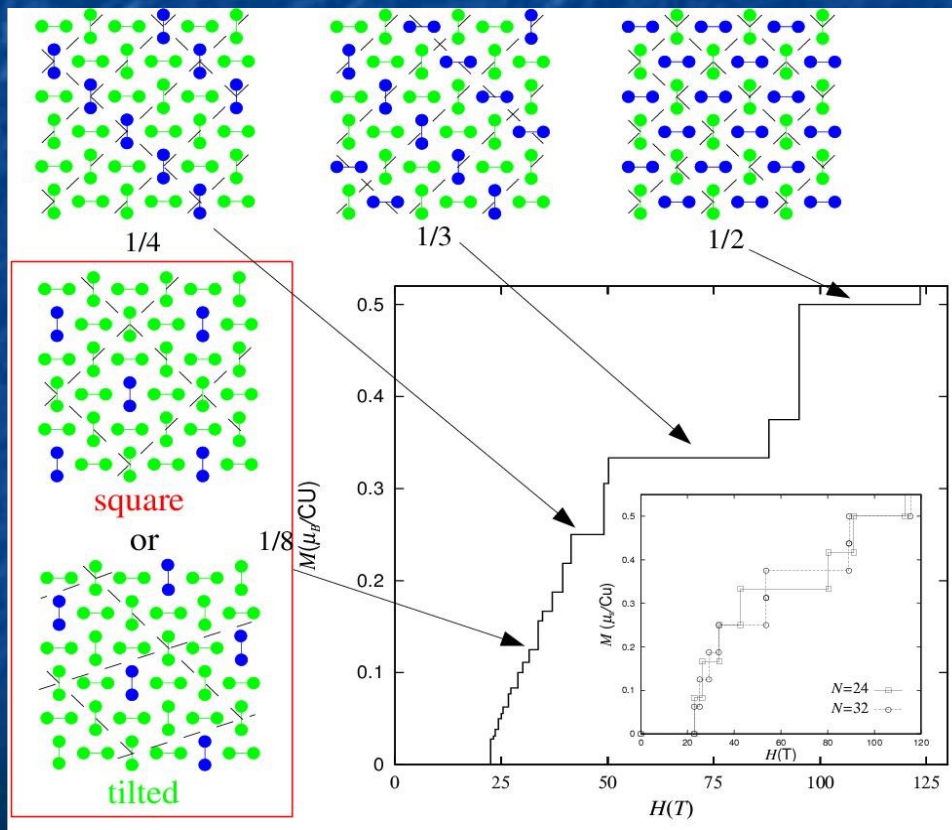
Triplet Repulsion



- Kinetic energy $\ll$ potential energy
- Long-range repulsion
 - Crystals of triplets with high commensurability
 - **Magnetization plateaux**

Superstructures at magnetization plateaus in $\text{SrCu}_2(\text{BO}_3)_2$

Shin Miyahara and Kazuo Ueda



- Simple ansatz for long-range triplet-triplet interaction
- Many plateaus

Magnetization plateaus of the Shastry-Sutherland model for $\text{SrCu}_2(\text{BO}_3)_2$: Spin-density wave, supersolid, and bound states

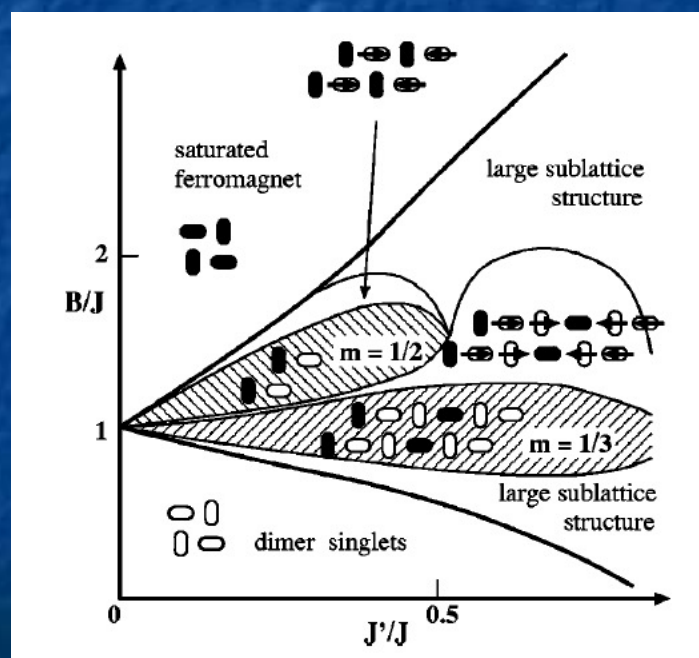
Tsutomu Momoi*

Lyman Laboratory of Physics, Harvard University, Cambridge, Massachusetts 02138

Keisuke Totsuka

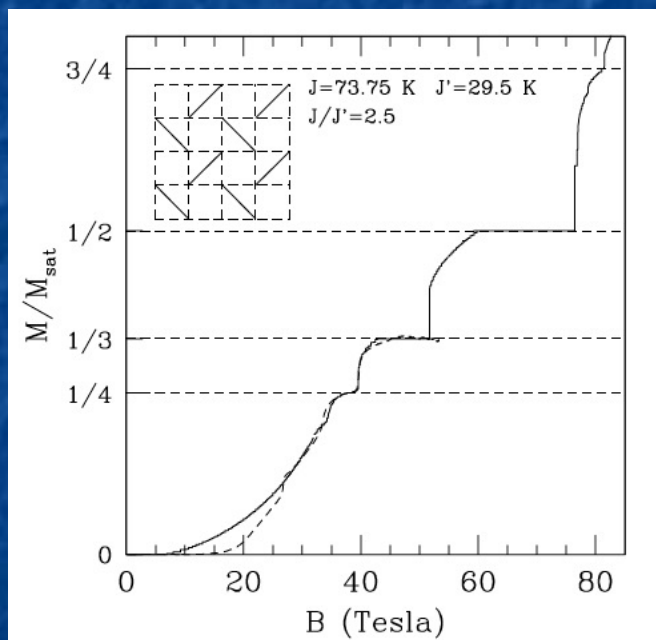
Department of Physics, Kyushu University, Hakozaki, Higashi-ku, Fukuoka-shi 812-8581, Japan

(Received 1 June 2000)



Magnetization Plateaus of $\text{SrCu}_2(\text{BO}_3)_2$ from a Chern-Simons Theory

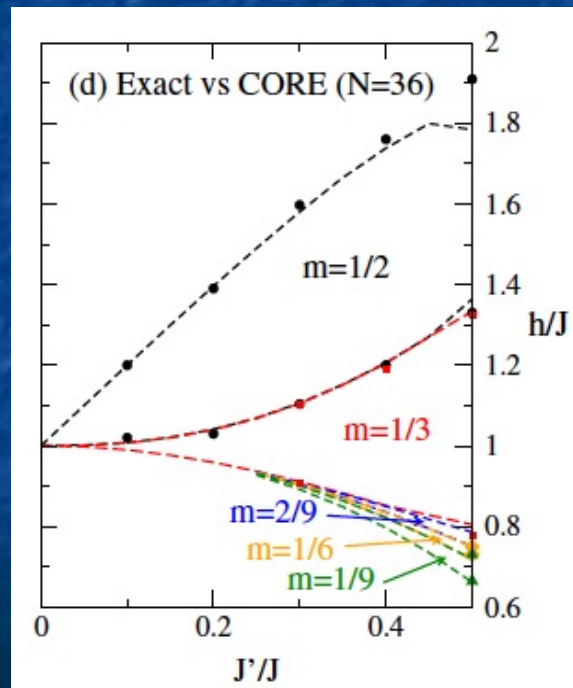
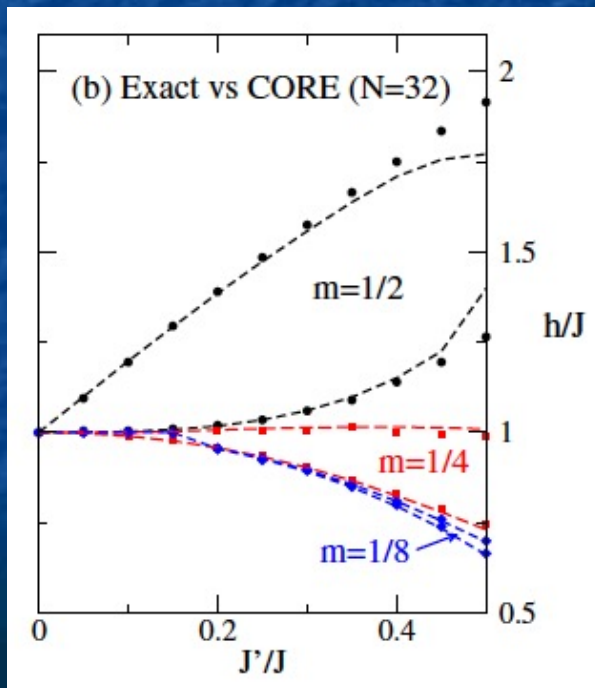
G. Misguich,¹ Th. Jolicoeur,² and S.M. Girvin^{3,4}



Effective Theory of Magnetization Plateaux in the Shastry-Sutherland Lattice

A. Abendschein^{1,2} and S. Capponi^{1,2,*}

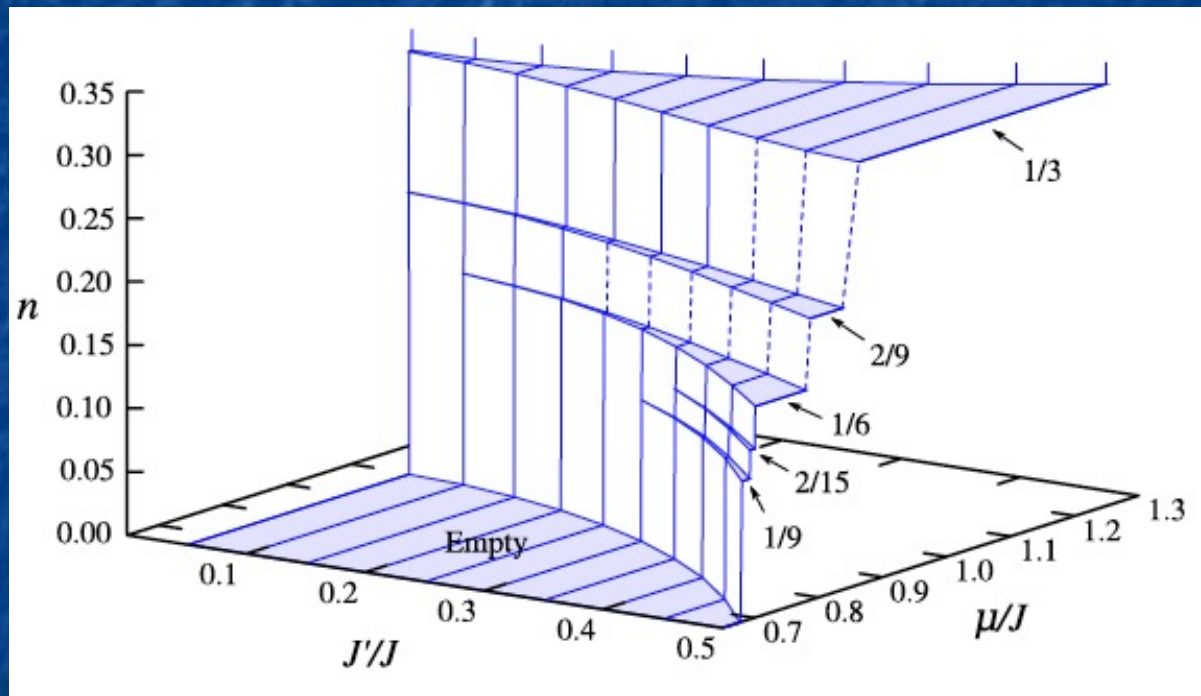
Effective model with CORE (Contractor Renormalization)
Exact diagonalization on small clusters



- Large finite-size effects
- No 2/15 plateau

Theory of Magnetization Plateaux in the Shastry-Sutherland Model

J. Dorier,¹ K. P. Schmidt,^{2,*} and F. Mila¹



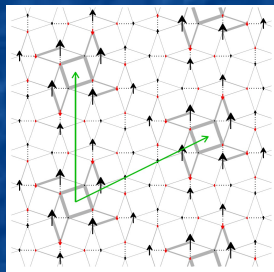
No $1/8$ plateau

Expansion in J'/J up to 0.5 using p-CUT
(perturbative continuous unitary transformation)

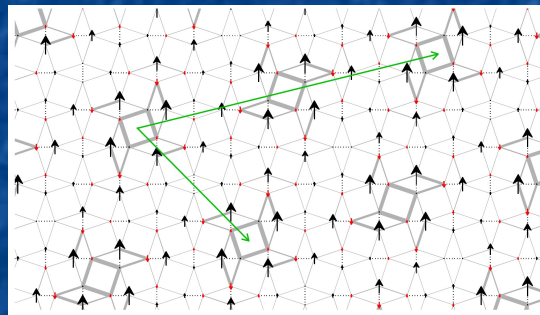
Crystals of Bound States in the Magnetization Plateaus of the Shastry-Sutherland Model

Philippe Corboz¹ and Frédéric Mila²

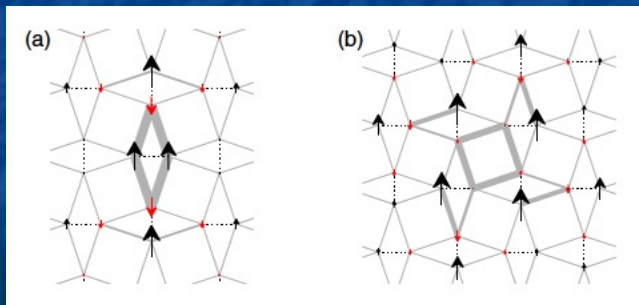
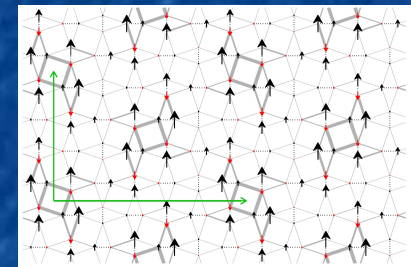
1/8



2/15

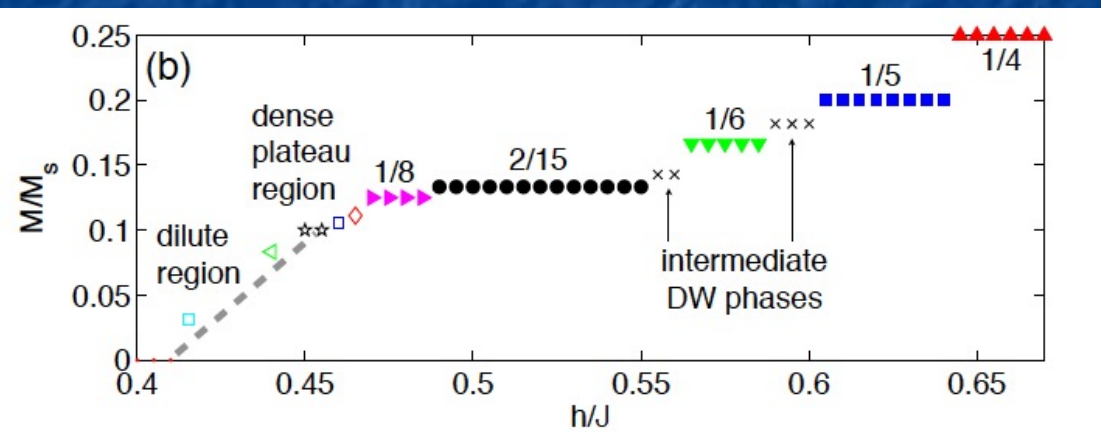


1/6



Triplet

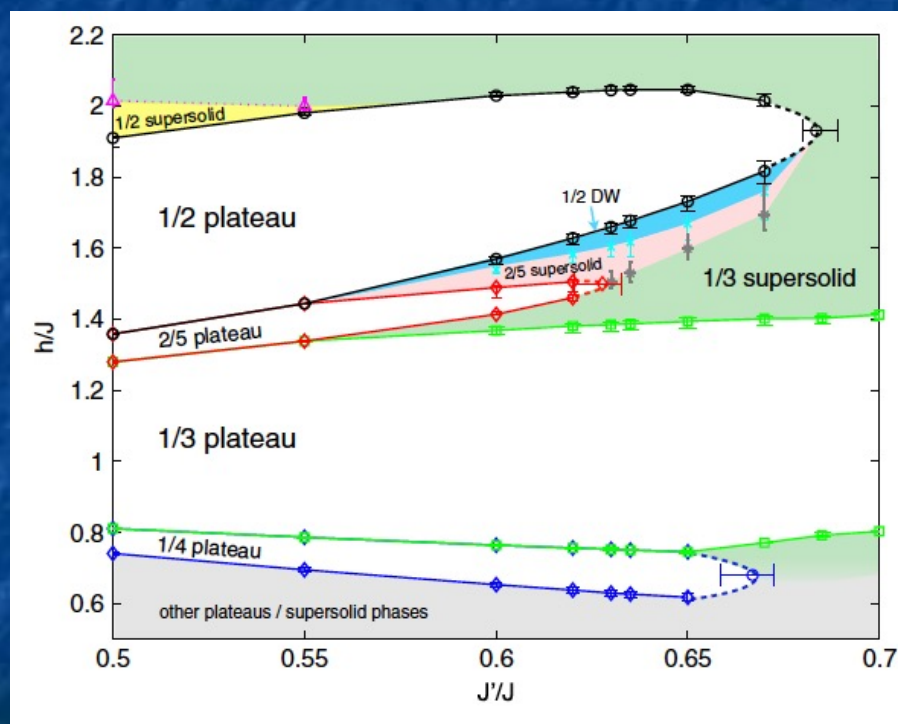
Spin-2
bound state



Method: iPEPS (tensor networks)

Magnetization of $\text{SrCu}_2(\text{BO}_3)_2$ in Ultrahigh Magnetic Fields up to 118 T

Y.H. Matsuda,^{1,*} N. Abe,¹ S. Takeyama,¹ H. Kageyama,² P. Corboz,³ A. Honecker,^{4,5} S.R. Manmana,⁴
G.R. Foltin,⁶ K.P. Schmidt,⁶ and F. Mila⁷



Scope

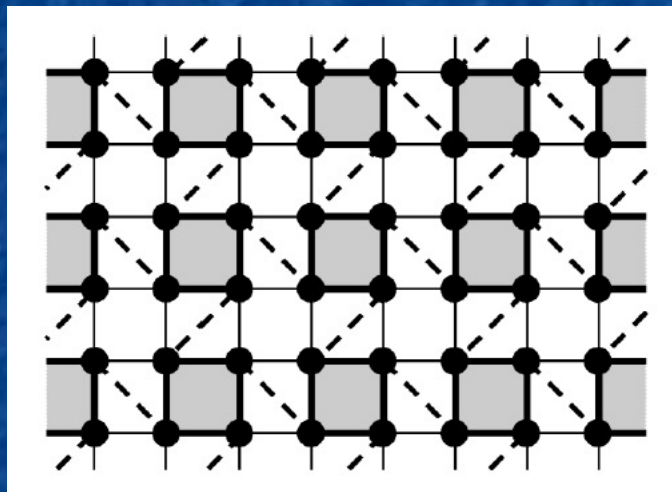
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Quantum Phase Transitions in the Shastry-Sutherland Model for $\text{SrCu}_2(\text{BO}_3)_2$

Akihisa Koga and Norio Kawakami

Department of Applied Physics, Osaka University, Suita, Osaka 565-0871, Japan

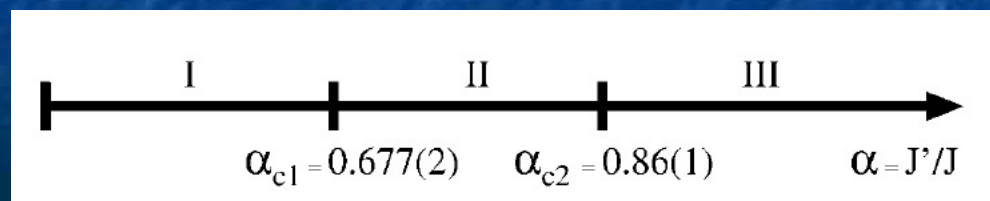
(Received 6 December 1999)



Series expansions



Intermediate
plaquette phase

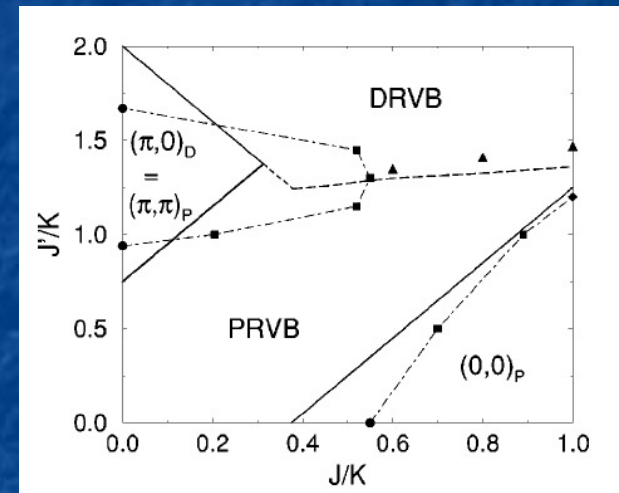
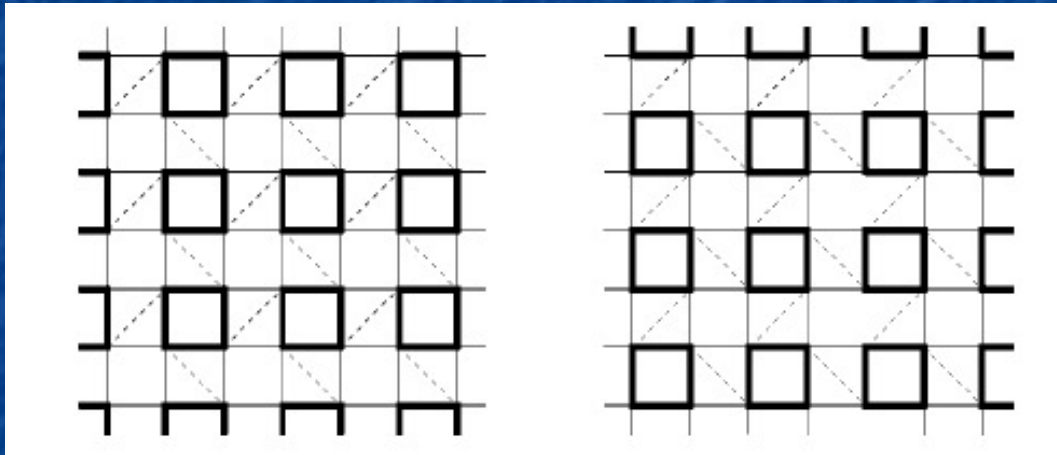


Phase diagram of the quadrumerized Shastry-Sutherland model

Andreas Läuchli, Stefan Wessel, and Manfred Sigrist

Institut für Theoretische Physik, ETH-Hönggerberg, CH-8093 Zürich, Switzerland

(Received 5 February 2002; published 20 June 2002)



Exact diagonalizations $\rightarrow$ two-fold degenerate plaquette phase

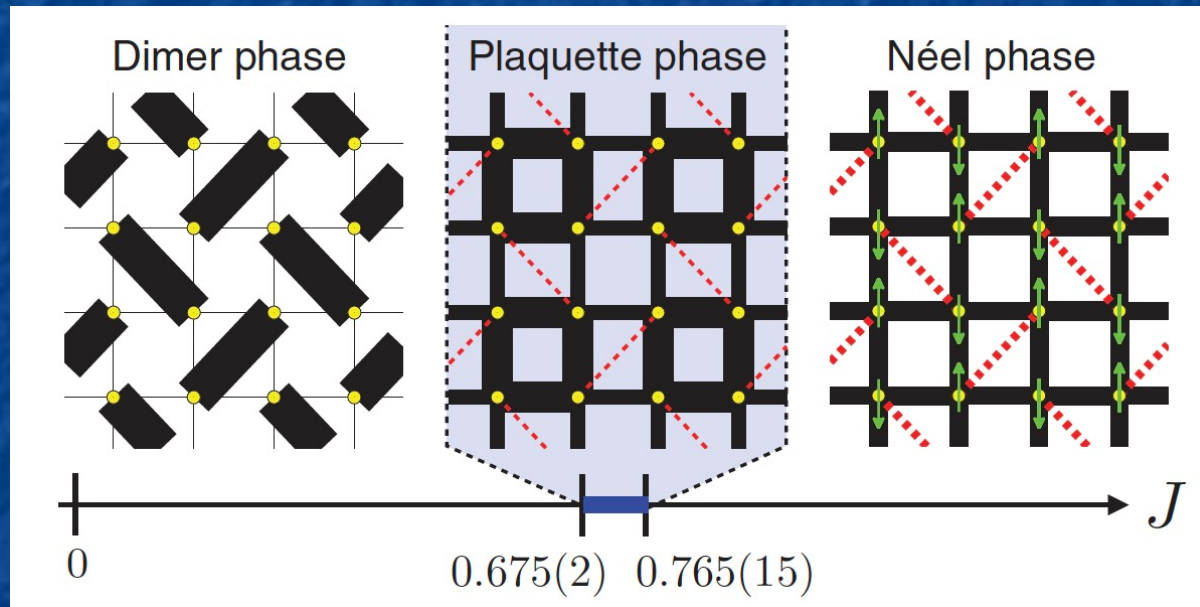
Tensor network study of the Shastry-Sutherland model in zero magnetic field

Philippe Corboz¹ and Frédéric Mila²

¹*Theoretische Physik, ETH Zürich, CH-8093 Zürich, Switzerland*

²*Institut de théorie des phénomènes physiques, École Polytechnique Fédérale de Lausanne (EPFL), CH-1015 Lausanne, Switzerland*

(Received 13 December 2012; revised manuscript received 27 February 2013; published 27 March 2013)



iPEPS with various setups and bond dimension up to 10

A Novel Ordered Phase in $\text{SrCu}_2(\text{BO}_3)_2$ under High Pressure

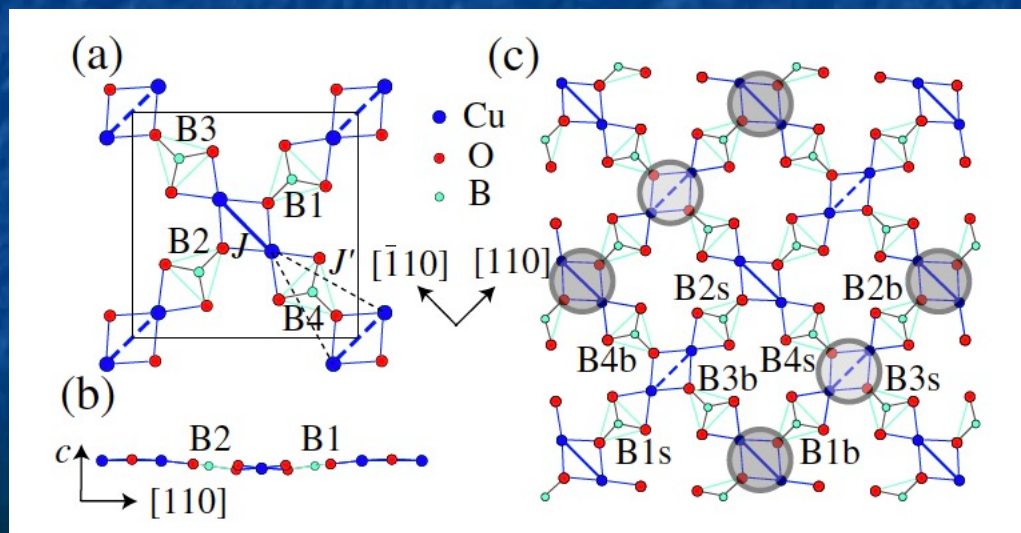
Takeshi WAKI^{1*}, Koichi ARAI^{1†}, Masashi TAKIGAWA^{1‡}, Yuta SAIGA^{1,2},
Yoshiya UWATOKO¹, Hiroshi KAGEYAMA³, and Yutaka UEDA¹

¹*Institute for Solid State Physics, The University of Tokyo, Kashiwa, Chiba 277-8581*

²*Graduate School of Science and Engineering, Saitama University, Saitama 338-8570*

³*Department of Chemistry, Graduate School of Science, Kyoto University, Kyoto 606-8502*

(Received May 2, 2007; accepted May 31, 2007; published July 10, 2007)



Intermediate phase
under pressure,
but **two types of
Cu sites**



NOT the plaquette phase

ARTICLE

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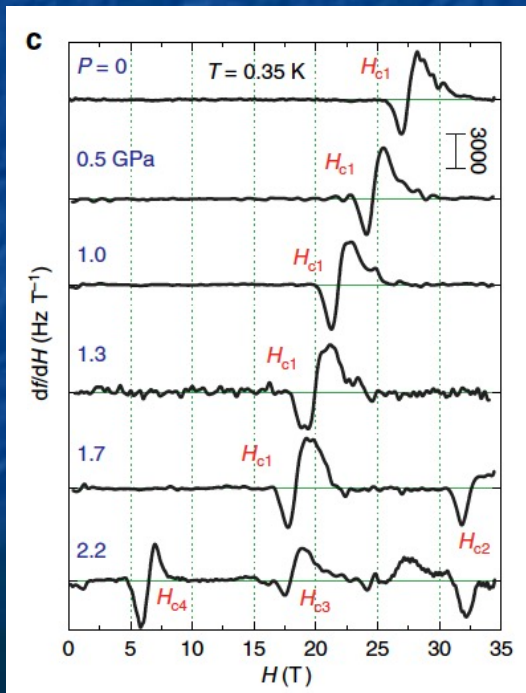
DOI: 10.1038/ncomms11956

OPEN

Crystallization of spin superlattices with pressure and field in the layered magnet $\text{SrCu}_2(\text{BO}_3)_2$

S. Haravifard^{1,2,3}, D. Graf⁴, A.E. Feiguin⁵, C.D. Batista^{6,7,8}, J.C. Lang³, D.M. Silevitch^{2,9}, G. Srajer³, B.D. Gaulin¹⁰, H.A. Dabkowska¹⁰ & T.F. Rosenbaum^{2,9}

Second derivative of magnetization



Magnetic field response
under pressure



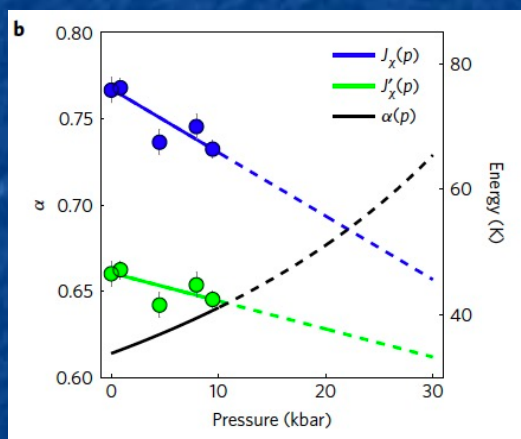
Confirmation of a phase
transition around 2GPa

4-spin plaquette singlet state in the Shastry–Sutherland compound $\text{SrCu}_2(\text{BO}_3)_2$

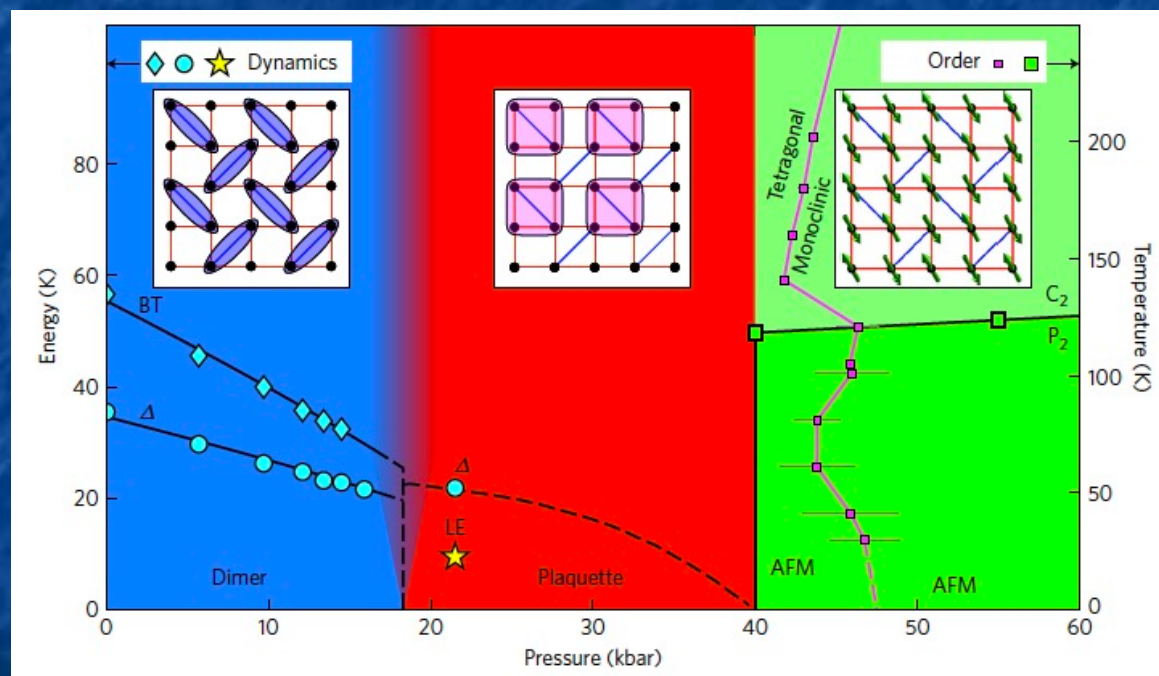
M. E. Zayed^{1,2,3*}, Ch. Rüegg^{2,4,5}, J. Larrea J.^{1,6}, A. M. Läuchli⁷, C. Panagopoulos^{8,9}, S. S. Saxena⁸, M. Ellerby⁵, D. F. McMorrow⁵, Th. Strässle², S. Klotz¹⁰, G. Hamel¹⁰, R. A. Sadykov^{11,12}, V. Pomjakushin², M. Boehm¹³, M. Jiménez-Ruiz¹³, A. Schneidewind¹⁴, E. Pomjakushina¹⁵, M. Stingaciu¹⁵, K. Conder¹⁵ and H. M. Rønnow¹

Neutron scattering

Susceptibility



J'/J increases

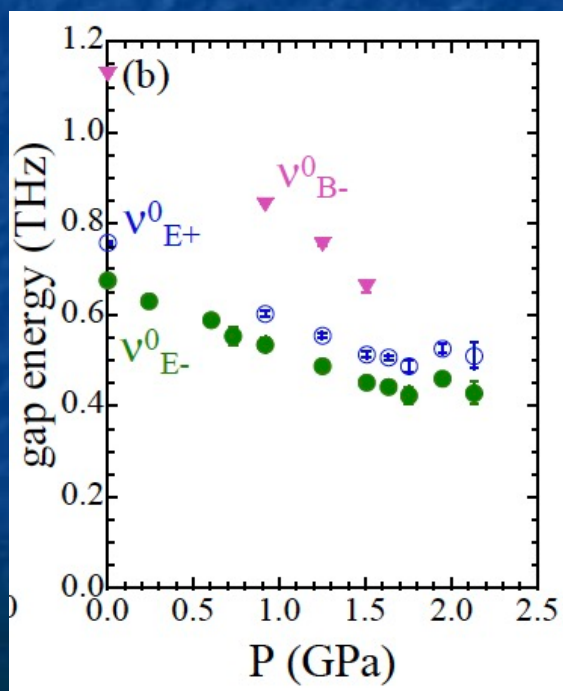


The intermediate phase is a full plaquette phase!

Direct Observation of the Quantum Phase Transition of $\text{SrCu}_2(\text{BO}_3)_2$ by High-Pressure and Terahertz Electron Spin Resonance

Takahiro Sakurai^{1*}, Yuki Hirao², Keigo Hijii³, Susumu Okubo³, Hitoshi Ohta³, Yoshiya Uwatoko⁴, Kazutaka Kudo⁵, and Yoji Koike⁶

ESR



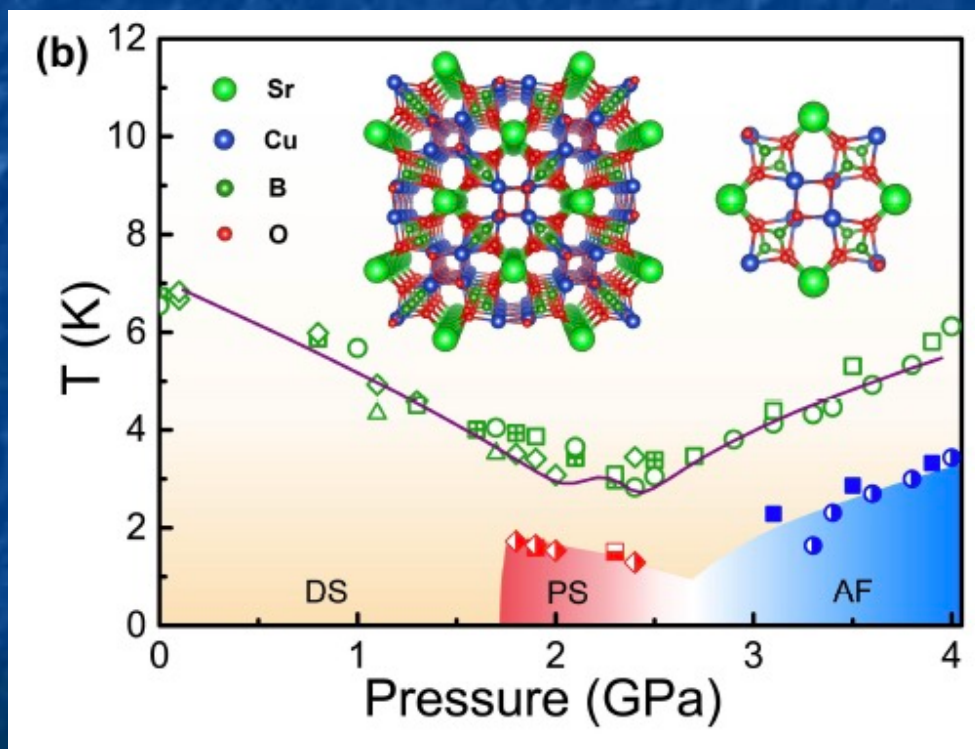
The gap levels off around 1.8 GPa



Confirmation of a phase transition around 1.8 GPa

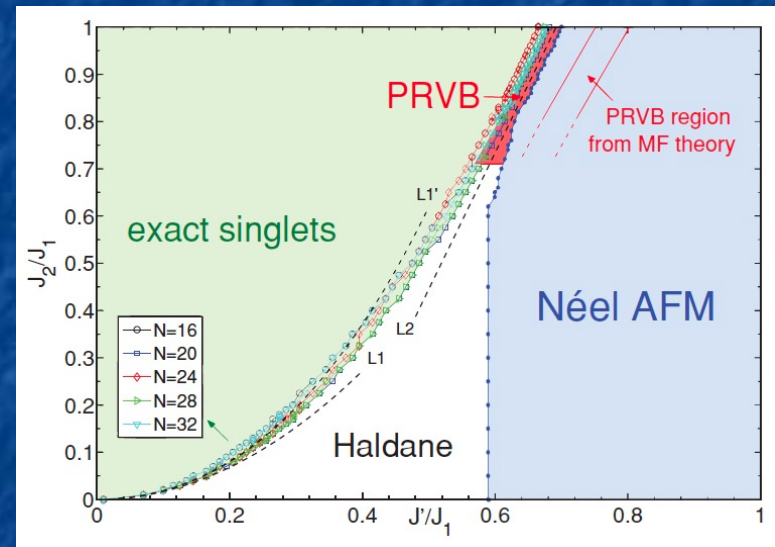
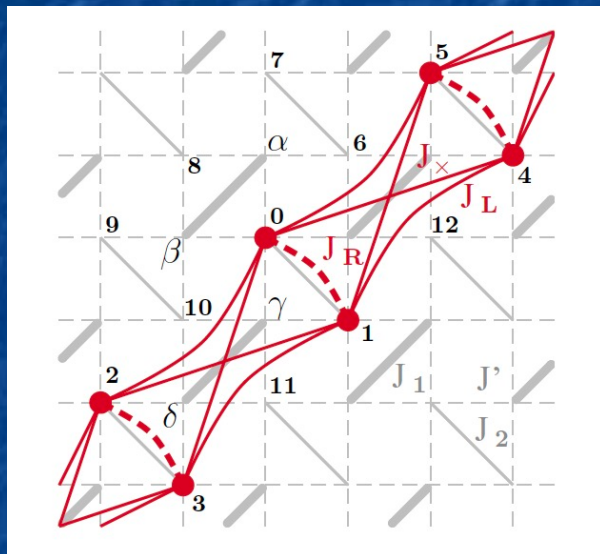
Quantum Phases of $\text{SrCu}_2(\text{BO}_3)_2$ from High-Pressure Thermodynamics

Jing Guo¹, Guangyu Sun^{1,2}, Bowen Zhao³, Ling Wang^{4,5}, Wenshan Hong^{1,2}, Vladimir A. Sidorov⁶, Nvsn Ma¹, Qi Wu¹, Shiliang Li^{1,2,7}, Zi Yang Meng^{1,8,7,*}, Anders W. Sandvik^{3,1,†} and Liling Sun^{1,2,7,‡}

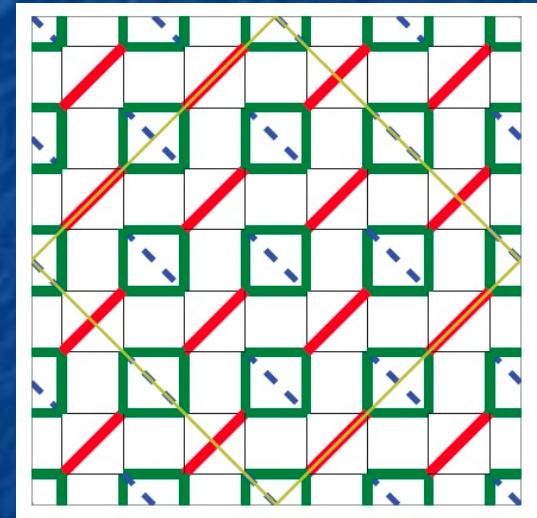
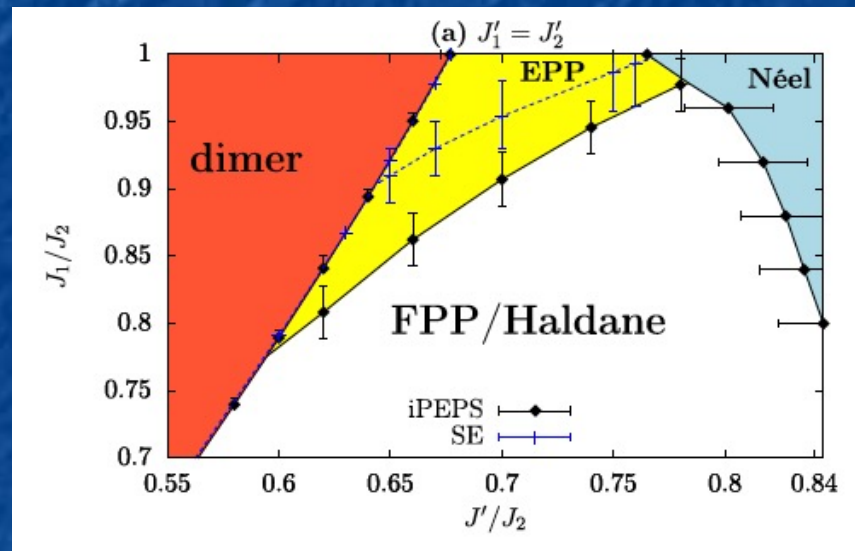


PHYSICAL REVIEW B 83, 140414(R) (2011)

Emergence of one-dimensional physics from the distorted Shastry-Sutherland lattice

M. Moliner,^{1,*} I. Rousochatzakis,^{2,†} and F. Mila^{3,‡}

$J_2 \ll J_1 \rightarrow$ effective fully frustrated ladder
 $\rightarrow$ **Haldane phase**

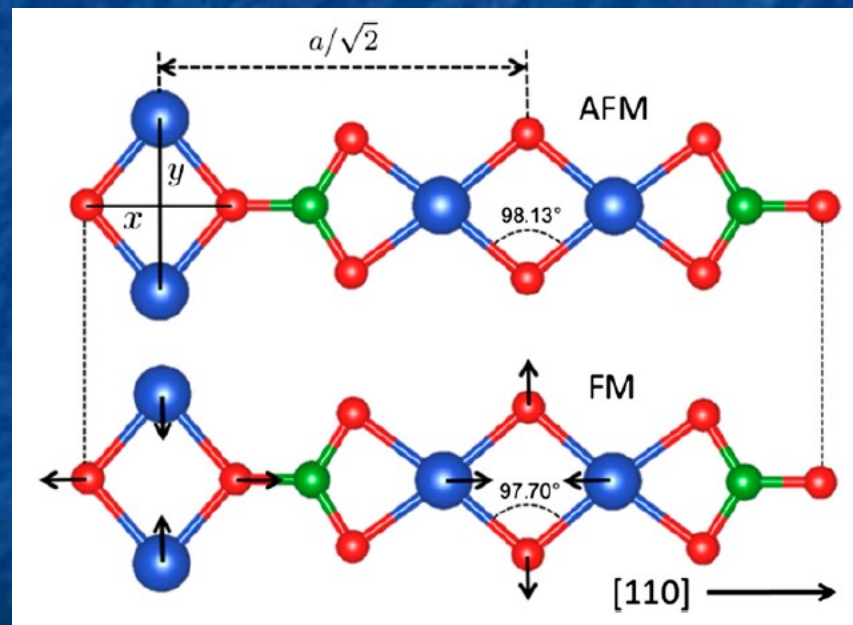
Competition between intermediate plaquette phases in $\text{SrCu}_2(\text{BO}_3)_2$ under pressureC. Boos,^{1,2,*} S. P. G. Crone,³ I. A. Niesen,³ P. Corboz,³ K. P. Schmidt,^{1,†} and F. Mila^{2,‡}

Haldane and full plaquette phases are adiabatically connected
 → single alternative to plaquette phase

Magnetic nanopantograph in the $\text{SrCu}_2(\text{BO}_3)_2$ Shastry–Sutherland lattice

Guillaume Radtke^a, Andrés Saúl^{b,c,1}, Hanna A. Dabkowska^d, Myron B. Salamon^{e,f}, and Marcelo Jaime^f

PNAS | February 17, 2015 | vol. 112 | no. 7 | 1971–1976



Scope

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- **Topological magnons**
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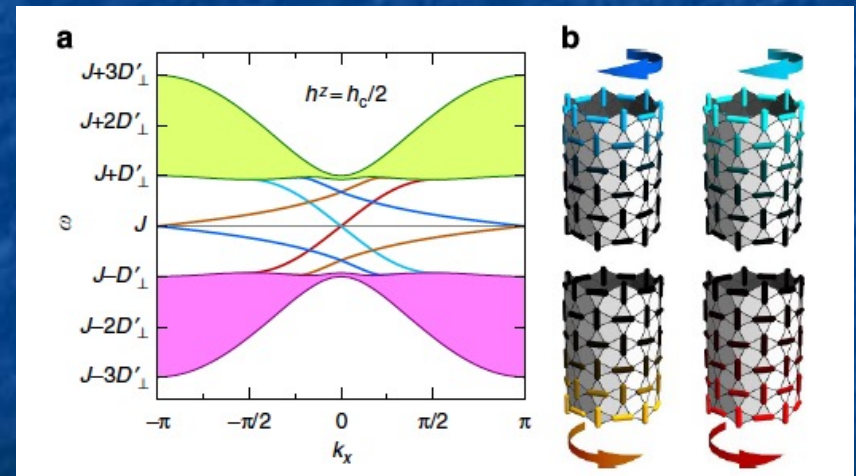
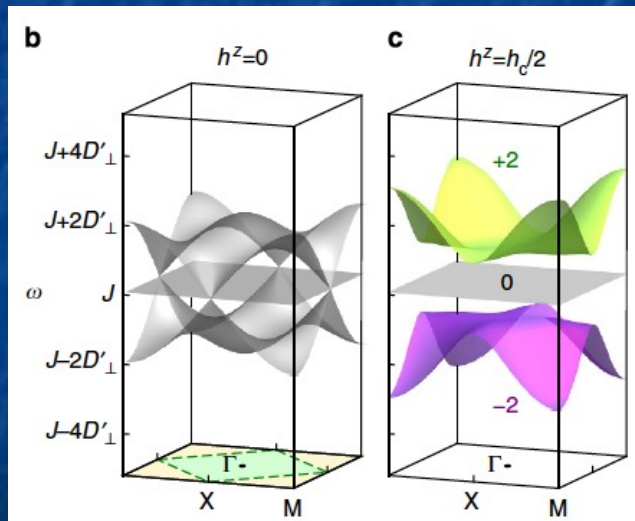
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Hall effect of triplons in a dimerized quantum magnet

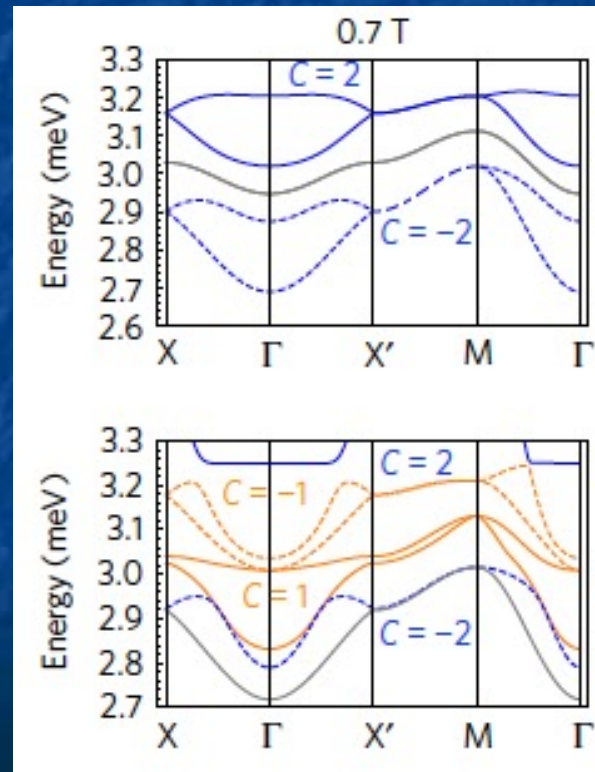
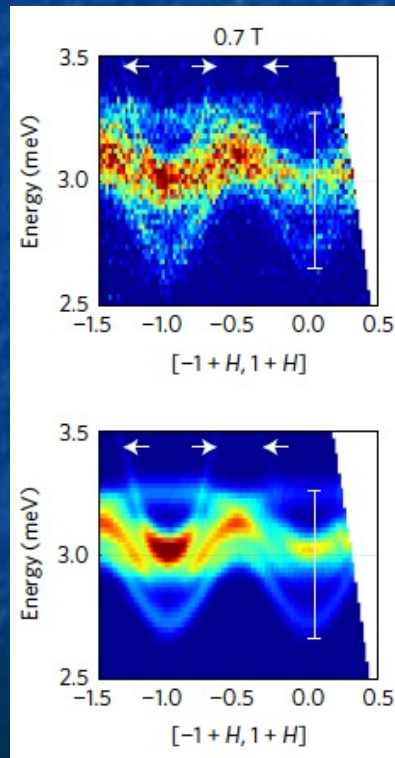
Judit Romhányi¹, Karlo Penc² & R. Ganesh¹



DM interactions + small magnetic field

Topological triplon modes and bound states in a Shastry–Sutherland magnet

P. A. McClarty^{1,2*}, F. Krüger^{1,3*}, T. Guidi¹, S. F. Parker¹, K. Refson^{1,4}, A. W. Parker⁵, D. Prabhakaran⁶ and R. Coldea⁶



Scope

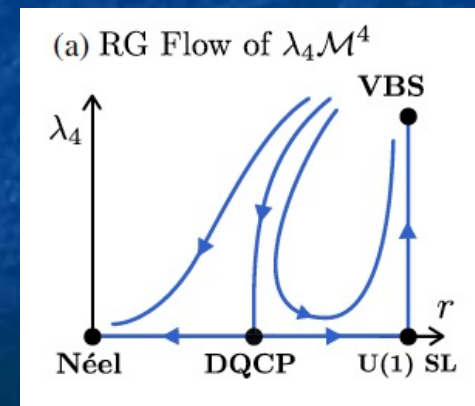
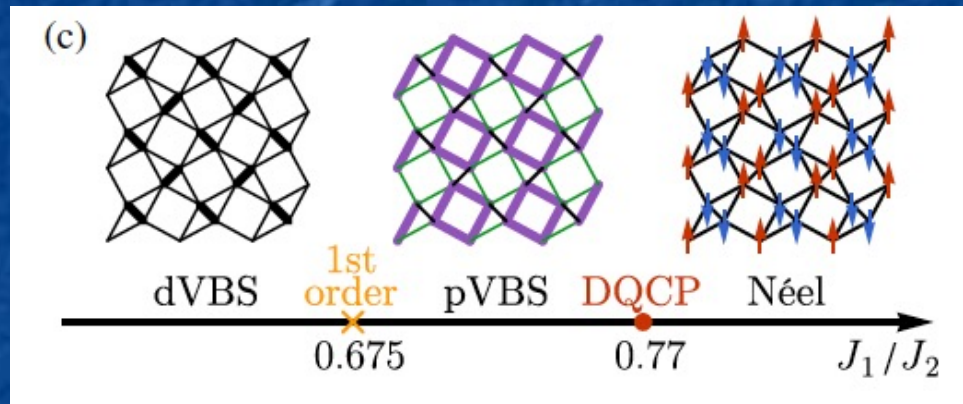
- The pioneers
Shastry-Sutherland 1981, Smith-Keszler 1991
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Signatures of a Deconfined Phase Transition on the Shastry-Sutherland Lattice: Applications to Quantum Critical $\text{SrCu}_2(\text{BO}_3)_2$

Jong Yeon Lee¹, Yi-Zhuang You,^{1,2} Subir Sachdev,¹ and Ashvin Vishwanath¹

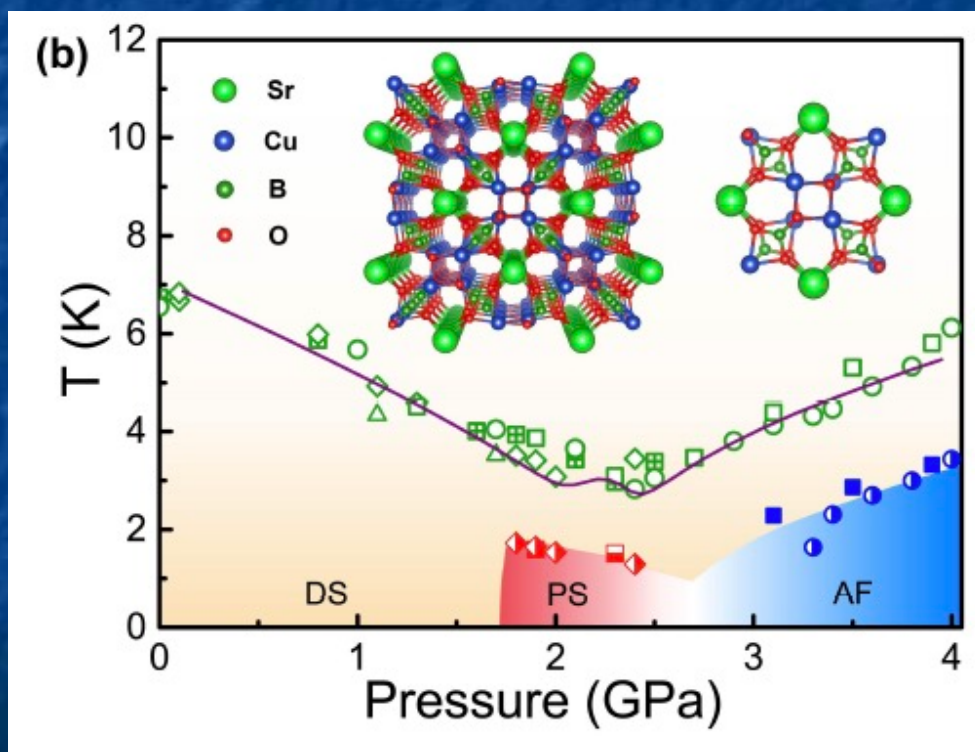
¹Department of Physics, Harvard University, Cambridge, Massachusetts 02138, USA

²Department of Physics, University of California, San Diego, California 92093, USA



Quantum Phases of $\text{SrCu}_2(\text{BO}_3)_2$ from High-Pressure Thermodynamics

Jing Guo¹, Guangyu Sun^{1,2}, Bowen Zhao³, Ling Wang^{4,5}, Wenshan Hong^{1,2}, Vladimir A. Sidorov⁶, Nvsen Ma¹, Qi Wu¹, Shiliang Li^{1,2,7}, Zi Yang Meng^{1,8,7,*}, Anders W. Sandvik^{3,1,†} and Liling Sun^{1,2,7,‡}

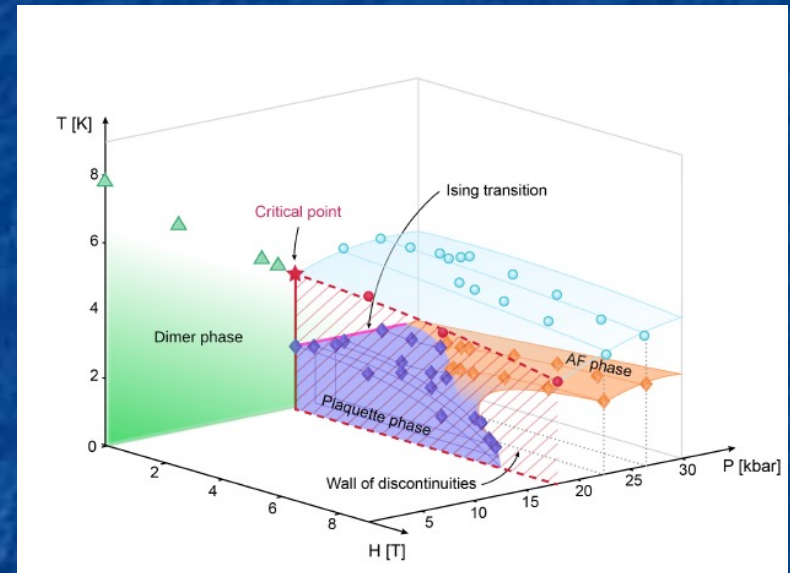
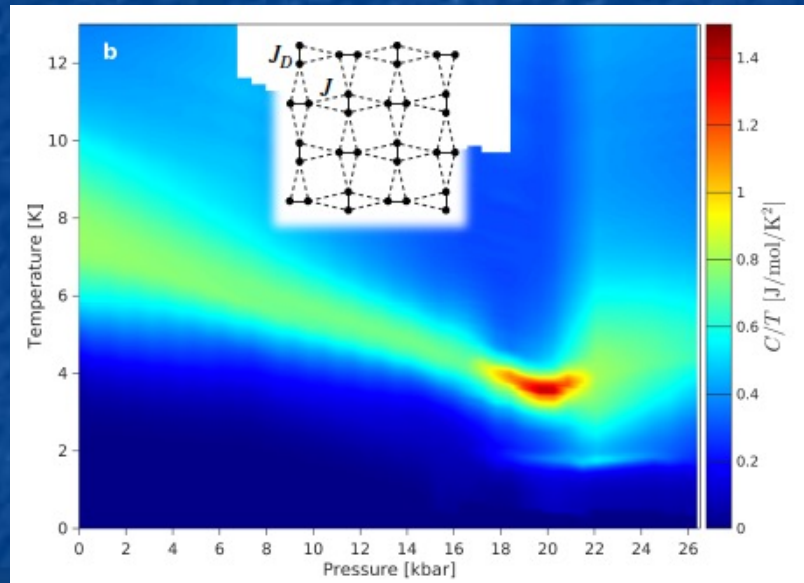


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A quantum magnetic analogue to the critical point of water

J. Larrea Jiménez,^{1,2} S. P. G. Crone,³ E. Fogh,² M. E. Zayed,⁴ R. Lortz,⁵ E. Pomjakushina,⁶ K. Conder,⁶ A. M. Läuchli,⁷ L. Weber,⁸ S. Wessel,⁸ A. Honecker,⁹ B. Normand,^{10,2} Ch. Rüegg,^{10,11,2,12} P. Corboz,³ H. M. Rønnow,² and F. Mila²



What else?

- Bound states
- Impurity effects
- Spin supersolid phases
- ...

$\text{SrCu}_2(\text{BO}_3)_2$ is the most interesting quantum magnet ever synthesized!